# Minimum Bias Event Shapes 

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## 1 Event Shape Observables

In order to investigate Minimum Bias events using observables, which describe distribution tracks from charged particles in the event one has several possibilities.

### 1.1 Transverse Thrust

Let's start with the observable called Transverse Thrust, which is defined as

$$
\begin{equation*}
T_{\mathrm{T}}=\max _{\vec{n}_{\mathrm{T}}} \frac{\sum_{i} \vec{p}_{\mathrm{T}, i} \cdot \vec{n}_{\mathrm{T}}}{\sum_{i} p_{\mathrm{T}, i}} \tag{1}
\end{equation*}
$$

where $\vec{p}_{\mathrm{T}}=\left(p_{x}, p_{y}\right)$ is the momentum transverse to the beam and $\vec{n}_{\mathrm{T}}=\left(n_{x}, n_{y}\right)$ is the transverse vector that maximizes the sum.

### 1.2 Transverse Spherocity

Another related observable is Transverse Spherocity defined as

$$
\begin{equation*}
S_{\mathrm{T}}=\frac{\pi^{2}}{4} \min _{\vec{n}_{\mathrm{T}}}\left(\frac{\sum_{i}\left|\vec{p}_{\mathrm{T}, i} \times \vec{n}_{\mathrm{T}}\right|}{\sum_{i} p_{\mathrm{T}, i}}\right)^{2} \tag{2}
\end{equation*}
$$

where $\vec{p}_{\mathrm{T}}=\left(p_{x}, p_{y}, 0\right)$ is the momentum transverse to the beam and $\vec{n}_{\mathrm{T}}=\left(n_{x}, n_{y}, 0\right)$ is the transverse vector that minimizes the sum

## 2 Finding Thrust Axis

In case of transverse observables, the task to find unit vector which maximizes the sum can be reduced to just one dimensional problem:

- Lets define $\vec{n}_{\mathrm{T}}=(\cos \phi, \sin \phi)$ or $\vec{n}_{\mathrm{T}}=(\cos \phi, \sin \phi, 0)$
- $\phi$ is angle from $x$-axis
- $T_{\mathrm{T}}$ and $S_{\mathrm{T}}$ are now dependent only on angle $\phi$
- $\vec{n}_{\mathrm{T}}$ in both cases found using 1D minimization method


## Appendices

A Mean $p_{\mathrm{T}}$

$$
\begin{equation*}
\left\langle p_{\mathrm{T}}\right\rangle=\frac{1}{N_{\mathrm{sel}}} \sum_{i}^{N_{\text {sel }}} p_{\mathrm{T}, i} \tag{3}
\end{equation*}
$$

## Info

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